Investigating Trigonometric Functions

The Reciprocal Functions [TrigFunc.gsp]

- **I.** Click on the section titled **"Cosecant Function"** (or click the tab at the bottom of the screen. Answer the following questions:
- 1. What is the range of $f(x) = \csc(x)$?____

2. Fill in the box with the appropriate trig. function: $\csc(x) = \frac{1}{|x|^2}$

3. Click on "Show sin(x)".

3.0

2:0

1.0

-1.0

- 4. On the *x*-interval 0 to 3, at what point are the functions f(x) = sin(x) and g(x) = csc(x) tangent to one another?
- 5. On the *x*-interval -5 to 5, how many times is $f(x) = \csc(x)$ asymptotic?______Approximate the decimal locations of the asymptotes______

6. Using the grid at the left, graph $g(x) = \csc(x)$ and $f(x) = \sin(x)$. Label the functions.

Name

Be careful that your *x*-values in full decimal form from Sketchpad and the *x*-values in radian notation on the graph grid represent the same values.

- **II.** Click on the section titled **"Secant Function"** (or click the tab at the bottom of the screen. Answer the following questions:
 - 1. What is the range of $f(x) = \sec(x)$?_____

 $\pi/2$

2. Fill in the box with the appropriate trig. function: $\sec(x) = \frac{1}{|x|}$

 $3\pi/2$

π

- 3. Click on "Show cos(x)".
- 4. On the *x*-interval -1 to 4, at what points are the functions f(x) = cos(x) and g(x) = sec(x) tangent to one another?
- 5. On the *x*-interval -6 to 3, how many times is $f(x) = \sec(x)$ asymptotic?______Approximate the decimal locations of the asymptotes______



6. Using the grid at the left, graph $g(x) = \sec(x)$ and $f(x) = \cos(x)$. Label the functions.

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III. Click on the section titled **"Cotangent Function"** (or click the tab at the bottom of the screen. Answer the following questions:

1. On the closed x-interval from 0 to 3, how many times is $f(x) = \cot(x)$ asymptotic ?

Approximate the decimal locations of the asymptotes _____

- 2. Fill in the box with the appropriate trig. function: $\cot(x) = \frac{1}{\left| \frac{1}{x} \right|^2}$
- 3. Click on "Show tan(x)".
- 4. On the *x*-interval 0 to 2, at what approximate decimal location is the function $f(x) = \tan(x)$ equal to the function $g(x) = \cot(x)$?

Approximately, what would this value be in radian notation?



5. Using the grid at the left, graph $g(x) = \cot(x)$ and $f(x) = \tan(x)$. Label the functions.

Be careful that your *x*-values in full decimal form from Sketchpad and the *x*-values in radian notation on the graph grid represent the same values.