Fibonacci Faces

Name

The Beautiful People



Need to know: The Golden Ratio, Phi (ϕ pronounced "fi") = 1.6180339891.

1.618033989. The ratio 1.6180339891: 1 is called the golden ratio, Phi. Use your graphing calculator to examine the tendency of the Fibonacci Sequence to approach the golden section. Enter the numbers from 1 to 12 in List 1 and the accompanying ratios in List 2. Produce a scatter plot. Enter Y1 = 1.618033989. Graph and examine.

1. 2/1	7
2. 3/2	8
3. 5/3	9
4. 8/5	10
5	11
6	12

Describe explicitly how the Fibonacci ratios relate to Phi. Be sure to describe "how" the values are approaching 1.618033989.

3. Phi, the golden ratio of 1.618033989, can be derived mathematically by solving the equation:

$$n^2 - n - 1 = 0.$$

Show that this equation can be solved algebraically to produce the value of Phi. Express your answer in fractional form. Do not use your calculator for a decimal solution to this equation. Use the calculator only to check.

4. Phi can be used to create some interesting equations. Which of the following statements relating to Phi are true?

- a.) $\phi^2 = \phi + 1$ _____
- b.) $1 / \phi = \phi 1$ _____
- d.) $\phi = 5^{0.5} * 0.5 + 0.5$
- 5. Phi can be used to compute any number of the Fibonacci Sequence, f(n), by using the formula: $f(n) = \phi^n / \sqrt{5}$

This formula will produce an estimate that will round to the correct Fibonacci number.

Using this formula, compute the indicated Fibonacci value:

- **a.**) 20th term _____
- **b.**) 35th term _____

Computing a more exact value needs a more intense formula: $f(n) = [\phi^n - (-\phi)^{-n}]/(2\phi - 1)$

Using this formula, compute the indicated Fibonacci value:

c.) 15th term _____

d.) 40th term _____